Stability of the Hecke algebra of wreath products

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Abstract

The non-abelian Hecke algebra $\mathcal{H}_{n,k}=\mathbb{C}[(S_k\wr S_n)\backslash S_{kn}/(S_k\wr S_n)]$ can be endowed with a filtration using the orbit structures of the elements $x\in S_{kn}$ relative to the action of S_{kn} on the set of k-partitions of $\{1,\cdots,kn\}$. We prove that the structure constants of the associated filtered algebra $\mathcal{F}_{n,k}$ is independent of n. This stability property leads to a universal algebra \mathcal{F} which governs the algebras $\mathcal{F}_{n,k}$. We also a prove that the structure constants of the algebras $\mathcal{H}_{n,k}$ is a polynomial in n.